Quantifying Marine Carbon Dioxide Removal via Alkalinity Enhancement Across Circulation Regimes Using ECCO-Darwin and 1D Models

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¹¹ Key Points:

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12	• Regional open-ocean alkalinity enhancement (OAE) is simulated in five archety-
13	pal ocean regimes using the data-assimilative ECCO-Darwin model.
14	• Ocean dynamics drive substantial regional differences in OAE efficiency.
15	• A 1D model is introduced to isolate and quantify OAE efficiency sensitivity to ver-
16	tical transport processes.

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18 Abstract

Ocean Alkalinity Enhancement (OAE) is emerging as a viable method for remov-19 ing anthropogenic CO_2 emissions from the atmosphere to mitigate climate change. To 20 achieve substantial carbon reductions, OAE would need to be deployed at scale across 21 the global ocean. Hence, there is a need to quantify how the efficiency of OAE varies glob-22 ally across a range of space-time scales in preparation for field deployments. Here we de-23 velop a marine carbon dioxide removal (mCDR) efficiency evaluation framework based 24 on the data-assimilative ECCO-Darwin ocean biogeochemistry model, which separates 25 and quantifies two key factors over seasonal to multi-annual timescales: 1) mCDR po-26 tential, which quantifies the ability of seawater to store additional carbon after an al-27 kalinity perturbation; and 2) dynamical mCDR efficiency, representing the impact of ocean 28 advection, mixing, and air-sea CO₂ exchange. We apply this framework to virtual OAE 29 deployments in five archetypal ocean circulation regimes with different mCDR poten-30 tials and dynamical efficiencies. The simulations highlight the importance of the dynam-31 ical factors, especially vertical transport, in driving differences in efficiency. To rapidly 32 isolate and quantify the factors that determine dynamical efficiency, we develop a reduced 33 complexity 1D model, rapid-mCDR. We show that combining the rapid-mCDR model 34 with existing ECCO-Darwin output allows for rapid characterization of OAE efficiency 35 at any location globally. Thus, these tools can be readily employed by research teams 36 and industry to model future field deployments and contribute to essential Monitoring, 37 Reporting, and Verification (MRV) efforts. 38

³⁹ Plain Language Summary

In an effort to counteract ongoing climate warming, engineering methods have been 40 proposed to artificially enhance marine carbon dioxide removal (mCDR) from the at-41 mosphere by reducing the ocean's acidity or enhancing its alkalinity — this is called Ocean 42 Alkalinity Enhancement (OAE). However, implementing OAE at a scale where it would 43 have a significant impact on the anthropogenic perturbation to atmospheric carbon diox-44 ide is costly and challenging, and many uncertainties remain regarding how effective OAE 45 would be. This paper addresses the practical question of where and when might OAE 46 be most effective, with a specific focus on exposing how regional variations in ocean cir-47 culation might lead to differences in the effectiveness of OAE. Several virtual scaled-up 48 regional and multi-decadal OAE deployments are simulated in five different open-ocean 49

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- ⁵⁰ circulation regimes in a state-of-the-art, global model of ocean circulation and biogeo-
- ⁵¹ chemistry. The results show that different ocean circulation regimes yield significant dif-
- ⁵² ferences in the effectiveness of OAE. These results help scientists and other stakehold-
- ers understand and quantify the range of possible impacts of circulation variability on
- 54 OAE efficiency.

55 1 Introduction

The major aim of the Paris Agreement is to reduce emissions and enhance carbon 56 sinks to keep the global temperature increase well below 2 degrees in this century (Rogelj 57 et al., 2018; Schimel & Carroll, 2024). This limit requires a 50% reduction in anthropogenic 58 carbon dioxide (CO_2) emissions by 2030, with net emissions nearly eliminated by 2050. 59 This effort will require almost complete decarbonization of the world's energy supply (Friedlingstein 60 et al., 2022; Palter et al., 2023). Furthermore, the IPCC's 6th assessment report has em-61 phasized that atmospheric CO_2 removal on the gigaton scale will be necessary to reach 62 net zero emissions (IPCC, 2022). 63

Due to the vast carbon reservoir (i.e. the mass of carbon) in the global oceans, which 64 is already a sink for roughly one quarter of anthropogenic CO₂ emissions (Gruber et al., 65 2019; Friedlingstein et al., 2022), various methods for marine carbon dioxide removal (mCDR) 66 have been proposed to accelerate the net transfer of carbon from the atmosphere to the 67 ocean (National Academies of Sciences, Engineering, and Medicine, 2022). Ocean Al-68 kalinity Enhancement (OAE; Renforth & Henderson, 2017) is one such method proposed 69 to bolster the uptake of atmospheric CO_2 by the ocean. Examples of particular OAE 70 approaches include: 1) reduction of seawater acidity through electrochemical processes 71 (House et al., 2007), 2) deployment of alkaline substances on the surface ocean, and 3) 72 enhanced weathering of alkaline minerals on land that accelerates their transfer to the 73 coastal ocean (Taylor et al., 2016; Montserrat et al., 2017). See Eisaman et al. (2023) 74 for a detailed technical review of various OAE approaches. Overall, National Academies 75 of Sciences, Engineering, and Medicine (2022) have rated OAE efficacy as "high confi-76 dence" with durability and scalability as "medium-high", yet the knowledge base remains 77 "low-to-medium". Thus, additional research to advance the knowledge base for OAE is 78 a priority. 79

The core principle of OAE leverages tight coupling between ocean alkalinity (Alk)80 and the nonlinear marine carbonate chemistry system (Middelburg et al., 2020). OAE 81 is generally focused on the deployment of Alk at, or near the ocean surface, which trans-82 forms aqueous carbon dioxide (CO₂) into bicarbonate (HCO₃⁻) and carbonate ions (CO₃²⁻) 83 through a series of rapid acid-base reactions (Zeebe & Wolf-Gladrow, 2001). This chem-84 ical adjustment leads to a reduction in aqueous carbon dioxide (CO_2^{aq}) concentrations 85 and thus lowers the partial pressure of carbon dioxide in seawater (pCO_2^{aq}) . If the Alk 86 addition and pCO_2^{aq} reduction occur in the surface ocean, it can drive ocean uptake of 87 CO_2 from the atmosphere or decrease the rate of CO_2 outgassing, both of which result 88 in a net increase in ocean carbon uptake. If the net CO_2 absorbed from the atmosphere 89 remains in the surface ocean, it tends to restore surface-ocean pCO_2^{aq} and therefore the 90 ocean-atmosphere pCO_2 gradient back toward the values it would have in the absence 91 of OAE deployment. The efficiency of OAE, which is typically defined by the ratio of 92 moles of CO_2 removed from the atmosphere per mole of deployed alkalinity, however, 93 remains poorly constrained. 94

For typical surface-ocean carbon chemistry, OAE has the potential to remove roughly 95 0.8 moles of CO₂ from the atmosphere per mole of deployed Alk (Renforth & Hender-96 son, 2017; Tyka et al., 2022). The actual amount of atmospheric CO_2 removed, however, 97 hinges on the complex interplay of ocean physics and biogeochemistry, and thus can de-98 viate from this value. While ocean carbonate chemistry reactions occur nearly instan-99 taneously and CO_2 in the atmosphere mixes efficiently on the timescale of days, the ad-100 justment of ocean pCO_2^{aq} perturbations to pre-deployment levels via air-sea CO_2 flux oc-101 curs over weeks to years (Jones et al., 2014; He & Tyka, 2023). This adjustment process 102 takes place against the backdrop of multi-scale ocean dynamics, with timescales rang-103 ing from seconds to thousands of years (Williams & Follows, 2011). Ocean dynamics strongly 104 influence the marine carbonate system state and can sequester OAE-perturbed waters 105 to depth far away from the air-sea interface, thereby reducing or delaying the removal 106 of atmospheric CO_2 and the efficiency of OAE. Furthermore, the total reduction of at-107 mospheric CO_2 can be smaller than the mCDR-driven sequestration, due to carbon cy-108 cle feedbacks with other components of the Earth System (see e.g., Tyka, 2024). 109

Several prior investigations have used numerical ocean models to show that the efficiency of OAE is subject to considerable regional and temporal variability across the global ocean and specifically that the ocean circulation significantly impacts OAE effi-

ciency (Ilyina et al., 2013; González et al., 2018; Burt et al., 2021; He & Tyka, 2023; Ya-113 mamoto et al., 2024). Most recently, Zhou et al. (2025) used a global ocean and sea-ice 114 model (Community Earth System Model version 2; CESM2), forced by atmospheric re-115 analysis, to quantify how ocean dynamics shape OAE efficiency globally. However, their 116 analysis was limited to pulse OAE experiments conducted for the year 1999, using a sin-117 gle model unconstrained by the ocean observations. Notably, CESM is known to exhibit 118 several biases, particularly in mixed layer depth — a factor that directly affects the re-119 sponse timescale to an OAE perturbation (Griffies et al., 2009; Danabasoglu et al., 2014; 120 Jones et al., 2014). As a result, some of their findings may not be fully representative 121 of real-world behavior. Consequently, key questions remain unresolved. For example: (1) 122 How does OAE efficiency vary across archetypal regional-scale circulation regimes? and 123 (2) How do spatial variations in efficiency evolve temporally under the influence of the 124 seasonal cycle and interannual climate variability? Fully addressing these high-priority 125 questions requires multi-model studies, and especially the use of data-constrained mod-126 els simulating a wide range of OAE scenarios. 127

In this study, we take a necessary step forward in building the knowledgebase needed 128 to answer these open questions by simulating regional-scale open-ocean OAE deployments 129 of monthly-to-multi-decadal duration in a data-constrained global model of ocean cir-130 culation, sea ice, and biogeochemistry/ecosystem dynamics, ECCO-Darwin (Carroll et 131 al., 2020, 2022, 2024). The data constraints significantly reduce ocean physical biases 132 that are common in unconstrained ocean models. For example, the representation of ocean 133 mixed layer depth in data constrained ECCO-Darwin model (Forget, Fukumori, et al., 134 2015; Forget, Campin, et al., 2015; ECCO Consortium et al., 2021) generally shows sig-135 nificantly better agreement with observations compared to unconstrained models (e.g. 136 Griffies et al., 2009; Tsujino et al., 2020; Treguier et al., 2023). We focus on regional and 137 multi-decadal scale deployments based on the hypothesis that they might achieve a "goldilocks" 138 trade-off: sufficiently small to be plausibly achievable vet sufficiently large to meaning-139 fully reduce global warming in the 21st century. We also consider continuous virtual OAE 140 simulations as a practical complement to monthly "pulse" OAE simulations, since con-141 tinuous experiments better characterize the typical efficiency of OAE as it varies sub-142 stantially with time, either seasonally or interannually. We elucidate the impact of ocean 143 dynamics on OAE efficiency by separating and comparing 1) the OAE potential, which 144 is calculated by assuming that the Alk perturbations remain in the surface layer of a hy-145

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pothetical static ocean and that air-sea exchange fully and instantly restores pCO_2^{aq} to 146 pre-deployment levels; and 2) the dynamic efficiency of OAE, which is computed by dif-147 ferencing the simulated ocean CO₂ flux from a counterfactual baseline simulation with-148 out OAE but having an otherwise identical dynamical ocean, normalized by OAE po-149 tential. Unlike previous studies (e.g. He & Tyka, 2023; Tyka, 2024), which combine both 150 OAE dynamical efficiency and potential into a single metric, we separate and individ-151 ually quantify the impact of these two key components in our analysis. We note there 152 is precedent for this separation of terms (Wang et al., 2023), with previous studies also 153 making a distinction between the maximum expected impact and the transient approach 154 to that impact (Yamamoto et al., 2024). We note that Yamamoto et al. (2024) take a 155 different approach to their computation by normalizing relative to direct air capture and 156 their efficiency term is dynamic, while the mCDR potential term is more implicit. 157

Although the efficiency of OAE is nominally different across space-time domains, 158 we build new understanding by presenting a series of five key case studies of OAE de-159 ployments at different locations, representative of distinct open-ocean circulation archetypes. 160 The regimes include a quiescent subtropical gyre contrasted with four energetic regimes, 161 including one in each of the following: a mid-latitude western boundary current, the Antarc-162 tic Circumpolar Current, a low-latitude equatorial upwelling region, and a high-latitude 163 deep-water formation region. Our results support the hypothesis that vertical transport 164 processes have an outsized impact on OAE efficiency. Hence, we isolate and more fully 165 quantify the sensitivity of OAE efficiency to vertical transport processes by developing 166 and analyzing a 1D vertical ocean biogeochemical model, called *rapid-mCDR*. 167

168 2 Methods

This section defines the metrics used to quantify mCDR efficiency by OAE (Section 2.1), describes the virtual OAE deployments and related numerical experiments (Section 2.2), reviews the ECCO-Darwin state estimate framework (Section 2.3), and presents the new 1D rapid-mCDR model for simulation of OAE-attribued Dissolved Inorganic Car-

bon (DIC) and Alk cycling and mCDR efficiency (Section 2.4).

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2.1 Metrics for Quantifying OAE-driven Atmospheric CO₂ Removal

¹⁷⁵ Net CO₂ removal from the atmosphere to the oceans ΔDIC_{tot} (in mol C) is eval-¹⁷⁶ uated by integrating the difference in CO₂ flux (Δf_C in mol C m⁻² s⁻¹) between OAE-¹⁷⁷ perturbed simulations (with alkalinity perturbation ΔAlk_{tot} in mol Alk) and the base-¹⁷⁸ line simulation, integrated over a discrete time interval t after deployment:

$$\Delta DIC_{tot}(t) = \int_{t_s}^{t_s+t} \int_A \Delta f_C \, \mathrm{d}A \, \mathrm{d}t, \tag{1}$$

with t_s marking the start of OAE deployment and A the global ocean surface area. Hence, Eq. 1 is equivalent to the volume integral of the OAE-perturbation to the local concentrations $\int_V \Delta DIC(t) dV$ over the ocean volume V where ΔDIC is the perturbation from the baseline DIC concentration (in mol C m⁻³). Throughout the paper, the subscript tot on DIC and Alk denotes total mass in the ocean (units of moles) in contrast to concentrations (units of mol m⁻³) in the absence of subscript tot.

In the numerical experiments presented here, the atmosphere is approximated as an infinite, imperturbable reservoir of CO_2 and the atmospheric and ocean physical states are unperturbed by OAE; the OAE-perturbation therefore acts to decrease pCO_2^{aq} . Other net ocean carbon chemistry responses to OAE are quantified similarly as differences between the OAE-perturbed and baseline simulations.

As in previous work (He & Tyka, 2023; Zhou et al., 2025), we define the practical measure of mCDR efficiency (η) as the ratio between the cumulative number of moles *DIC* absorbed by the ocean and cumulative number of moles *Alk* that were added to the surface ocean:

$$\eta(t) = \frac{\Delta DIC_{tot}(t)}{\Delta Alk_{tot}(t)},\tag{2}$$

where the time-dependent $\Delta DIC_{tot}(t)$ is calculated from simulation output using Eq. 1 and time-dependent $\Delta Alk_{tot}(t)$ is calculated from simulation forcing, which can be expressed as a surface-ocean alkalinity flux perturbation per unit time and deployment area (A_d) associated with the OAE introduced $Alk \Delta f_A$:

$$\Delta Alk_{tot}(t) = \int_{t_s}^{t_s+t} \int_{A_d} \Delta f_A \, \mathrm{d}A \, \mathrm{d}t.$$
(3)

Again, Eq. 3 is equivalent to the volume integral of the OAE-perturbation in the local 198 concentrations $\int_V \Delta A lk(t) dV$ over the ocean volume V. We note that if a given alka-199 linity perturbation ΔAlk_{tot} is added instantaneously and uniformly to a surface-ocean 200 area A_d at a time t_s , $\Delta f_A = \delta(t - t_s) \Delta A l k_{tot} / A_d$, where $\delta(t)$ is the Dirac delta func-201 tion. We note that our definition of efficiency $\eta(t)$ in Eq. 2 and in He and Tyka (2023) 202 are equivalent. Throughout the paper, a variety of metrics like η will be used that for-203 mally have units of moles DIC per mole Alk, and this mole per mole unit will be im-204 plied but not stated explicitly. 205

To provide insight into the mechanisms regulating η , we next characterize and separate the contributions of the OAE perturbation ΔAlk_{tot} and the mCDR response ΔDIC_{tot} to $\Delta p CO_2^{aq}$, following Takahashi et al. (1993):

$$\Delta p \operatorname{CO}_{2}^{aq} \approx \frac{\partial p \operatorname{CO}_{2}^{aq}}{\partial DIC} \frac{\Delta DIC_{tot}}{V} + \frac{\partial p \operatorname{CO}_{2}^{aq}}{\partial Alk} \frac{\Delta Alk_{tot}}{V}.$$
(4)

To ensure the accuracy of this expression, the perturbations ΔDIC_{tot} and ΔAlk_{tot} should be small and evenly distributed over a volume V with approximately constant sensitivities $\partial p CO_2^{aq} / \partial DIC$ and $\partial p CO_2^{aq} / \partial Alk$. Other factors that are typically important drivers of variability in $p CO_2^{aq}$, such as temperature and salinity, are identical in the OAE-perturbed and baseline simulations and thus do not appear in Eq. 4.

A useful relationship, which we call mCDR potential, can be defined as a ratio of net CO₂ uptake ($\Delta DIC_{tot,pot}$) and the amount of alkalinity added (ΔAlk_{tot}) to seawater, assuming complete air-sea equilibration of the alkalinity perturbation by substituting $\Delta p CO_2^{aq} = 0$ into Eq. 4 and rearranging:

$$mCDR_{pot} \equiv \frac{\Delta DIC_{tot,pot}}{\Delta Alk_{tot}} = -\frac{\partial pCO_2^{aq}}{\partial Alk} \left(\frac{\partial pCO_2^{aq}}{\partial DIC}\right)^{-1} = -\frac{DIC}{Alk} \frac{\gamma_{Alk}}{\gamma_{DIC}},\tag{5}$$

where $\Delta DIC_{tot,pot}$ is defined to be the ΔDIC_{tot} required to adjust pCO_2^{aq} to the baseline state; i.e., $\Delta pCO_2^{aq} = 0$. The pCO_2^{aq} sensitivities to DIC and Alk are $\gamma_{DIC} = \frac{DIC}{pCO_2^{aq}} \frac{\partial pCO_2^{aq}}{\partial DIC}$ and $\gamma_{Alk} = \frac{Alk}{pCO_2^{aq}} \frac{\partial pCO_2^{aq}}{\partial Alk}$ (e.g. Sarmiento & Gruber, 2006, page 329), and γ_{DIC} is the familiar buffer or Revelle factor (Takahashi et al., 1980). Typical latitude dependencies or maps of DIC, Alk, γ_{DIC} , and γ_{Alk} can be readily found in textbooks and published literature, for example in Takahashi et al. (1993) or Chapter 8 of Sarmiento and Gruber (2006). We note that our definition of mCDR potential differs from that of Wang et al. (2023), who use CDR potential to refer to the total DIC uptake for a given alkalinity injection, i.e., $\Delta DIC_{tot,pot}$ in our terminology. Our definition, in which the potential represents the DIC uptake per unit Alk injected, highlights the intrinsic dependence of the potential on the unperturbed ocean baseline state and facilitates easier comparisons between experiments with different magnitudes of injected alkalinity.

Since the $mCDR_{pot}$ defined by Eq. 5 varies across time and space, it is necessary to average values to obtain a single representative numeric estimate of $mCDR_{pot}$. The potential carbon removal $\Delta DIC_{tot,pot}$ for a given OAE experiment can be then expressed as:

$$\Delta DIC_{tot,pot}(t) \approx \langle mCDR_{pot} \rangle \Delta Alk_{tot}(t), \tag{6}$$

where the brackets around $\langle mCDR_{pot} \rangle$ indicate a space-time average of surface-ocean $mCDR_{pot}$ in the baseline simulation where and when the alkalinity is deployed. We quantify $mCDR_{pot}$ in Eq. 5 offline using Python toolbox for solving the marine carbonate system (*PyCO2SYS*; Humphreys et al., 2022) and the relevant gridded output from the baseline ECCO-Darwin simulation, as well as with the OceanSODA-ETHZ dataset (Gregor & Gruber, 2021) for comparison (see Supporting Information Text S2).

Hypothetically, $mCDR_{pot} = \eta$ and $\Delta DIC_{tot,pot} = \Delta DIC_{tot}$ if 1) all ΔAlk re-241 mains in the surface-ocean layer at the location where it is injected and 2) the air-sea 242 CO_2 flux perturbation Δf_C transfers exactly the atmospheric CO_2 needed to restore the 243 OAE-perturbated $\Delta p CO_2^{aq}$ to zero. However, it will be shown that the efficiency of OAE 244 η is typically (but not always) substantially less than $mCDR_{pot}$, even over decadal timescales. 245 This is primarily because OAE-perturbed waters can be isolated from atmospheric ex-246 change for up to thousands of years (England, 1995) via downward ocean transport and 247 mixing driven by circulation dynamics. Hence, we define the dynamical mCDR efficiency 248 249 as:

$$mCDR_{eff}(t) = \frac{\eta(t)}{\langle mCDR_{pot} \rangle}.$$
(7)

Eq. 7 separates η into a product of potential $(mCDR_{pot})$ and dynamical-efficiency ($mCDR_{eff}$) components, which provides a meaningful separation into drivers relating to carbon chemistry and ocean dynamics, respectively. The time dependence of $mCDR_{eff}$ or η is governed by the type of OAE deployment, particularly by the temporal evolution of the deployed alkalinity.

In order to evaluate the significance of vertical transport of OAE-modified waters and specifically the extent to which their mCDR potential has been realized as a function of space and time, we define $mCDR_{equil}$, following Wang et al. (2023). $mCDR_{equil}$ is a space-time resolved version of $mCDR_{eff}$, where ΔDIC_{tot} and ΔAlk_{tot} are replaced with local ΔDIC and ΔAlk concentrations:

$$mCDR_{equil} = \frac{1}{\langle mCDR_{pot} \rangle} \frac{\Delta DIC}{\Delta Alk}.$$
(8)

 $mCDR_{equil} \text{ values of one indicate that the mCDR has been fully realized relative}$ to the potential where the alkalinity was deployed, while values closer to zero suggest that only a small fraction of that potential has been achieved. To better understand the vertical extent of OAE-modified waters, we will show the vertical distribution of horizontallyaveraged $mCDR_{equil}$ values for select deployments. All points where $\Delta Alk = 0$ are omitted from the calculation.

Finally, in order to better characterize overall mCDR efficiency of deployment location and seasonality/interannual variability of net CO₂ uptake for continuous OAE experiments with a time-constant Alk flux f_A over many years, we define $mCDR_{eff}^p$:

$$mCDR_{eff}^{p}(t) = \frac{1}{\langle mCDR_{pot} \rangle} \frac{\partial/\partial t \ \Delta DIC_{tot}}{\partial/\partial t \ \Delta Alk_{tot}} = \frac{1}{\langle mCDR_{pot} \rangle} \frac{\int_{A} \Delta f_{C}(t) \, \mathrm{d}A}{A_{d} \ \Delta f_{A}},\tag{9}$$

which is the ratio of the OAE-perturbed CO₂ flux to the *Alk* flux at a given time normalized by $mCDR_{pot}$ (rather than integrating the fluxes in time since the beginning of the experiment as in $mCDR_{eff}$ and η). Thus, $mCDR_{eff}^{p}(t)$ is a rate-based measure of efficiency at a given time, whereas $\eta(t)$ and $mCDR_{eff}(t)$ are cumulative ocean reservoirbased measures of efficiency at a given time. The superscript 'p' stands for "pulse" for reasons described below in Section 2.2.5.

Symbol/Term	Brief Explanation	Section Guide
mCDR _{pot}	mCDR potential, net CO_2 uptake per unit of de-	Section 2.1
	ployed alkalinity assuming instantaneous and com-	
	plete adjustment of ocean $p\mathrm{CO}_2^{aq}$ with respect to the	
	unperturbed baseline situation via air-sea CO_2 flux	
η	A cumulative measure of net CO_2 uptake efficiency	Section 2.1
	per unit of deployed alkalinity based on the OAE-	
	perturbed ocean reservoirs of alkalinity and carbon	
$mCDR_{eff}$	A cumulative measure of the dynamical efficiency of	Section 2.1
	OAE relative to its potential	
$mCDR_{equil}$	A local, space-time resolved measure of the dynamical	Section 2.1
	efficiency of OAE relative to its potential at the de-	
	ployment location	
$mCDR_{eff}^p$	A rate-based measure of the efficiency of OAE com-	Section 2.2.5
	puted from the continuous OAE experiments, but	
	designed to represent the efficiency of pulse experi-	
	ments.	
Baseline Simulation	Unperturbed ECCO-Darwin state estimate, represent-	Section 2.3
	ing real-world ocean conditions	
Continuous Experiment	Persistent, steady OAE injection flux over multiple	Section 2.2.3
	years	
Pulse Experiment	A transient or instantaneous OAE injection flux	Section 2.2.4
rapid-mCDR(DeployAve)	Reduced-complexity rapid-mCDR model results ne-	Section 2.4
	glecting horizontal transport	
rapid-mCDR(TransAve)	Rapid-mCDR model results accounting for horizontal	Section 2.4
	transport	

 Table 1. List of key terms/quantities and the associated sections in this paper.

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2.2 Virtual OAE deployments

In this section, we describe our numerical experiments, including the baseline simulation and a suite of regional continuous and pulse OAE deployment scenarios that provide the basis for estimating the metrics described in Sec. 2.1 and answering the questions posed in the Introduction.

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2.2.1 Baseline simulation

The impacts and net CO_2 uptake attributed to OAE are evaluated with respect 281 to the baseline simulation. This *baseline* simulation of the full time-evolving global phys-282 ical and biogeochemical state, including the air-sea CO_2 flux and surface-ocean carbon-283 ate state necessary for calculating the metrics in Sec. 2.1, represents the natural ocean 284 state in the absence of any OAE perturbations from January 1, 1995 to December 31, 285 2017. The simulation is similar to several previous runs of ECCO-Darwin, which gen-286 erally agree well with in-situ observations over the global ocean and in various OAE de-287 ployment sites (see Supporting Information Text S1 and Figs. S1–S2). The methods un-288 derpinning ECCO-Darwin are briefly summarized in Sec. 2.3. 289

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2.2.2 OAE deployment sites

Five deployment regions were chosen to be representative of diverse dynamical and biogeochemical open-ocean conditions that serve as archetypes to help us build understanding of how various ocean circulation regimes impact OAE efficiency. Figure 1 and Table 2 describe the chosen OAE deployment sites. The Supporting Information Figs. S3 and S2 illustrate the surface ocean context of the five regions and demonstrate that ECCO-Darwin provides a realistic representation of surface ocean conditions.

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The following five mCDR experiments are considered:

• The North Atlantic Subduction (NAS) experiment represents unique conditions found in subpolar regions associated with subduction driven by heat loss, sea-ice formation and brine rejection, strong seasonally-driven vertical mixing, and seasonal biological CO₂ uptake.



Figure 1. OAE deployment sites considered in this study.

- The Western Boundary Current (WBC) experiment is representative of mid-latitude 302 conditions with strong horizontal currents and shear, along with intense vertical 303 mixing. 304 • The Antarctic Circumpolar Current (ACC) experiment represents conditions found 305 in the Southern Ocean, which are associated with strong zonal currents, seasonal 306 sea-ice cover, large-scale upwelling fronts, and seasonal biological uptake. 307 • The Equatorial Upwelling (EU) experiment is centered over the narrow upwelling 308 zone of the Tropical Pacific Ocean and is characterized by strong CO₂ outgassing 309 and biological uptake; its interannual variability tends to be dominated by El Niño-Southern 310 Oscillation events (ENSO), which are significant relative to the seasonal cycle. 311 • The Subtropical Gyre (STG) experiment is centered over a region dominated by 312 relatively slow surface-ocean currents and weaker primary production. It is po-313 sitioned near the eastern margin of the North Pacific Subtropical Gyre, mainly 314 because site selection closer to land should enhance deployment feasibility. 315
- 316

2.2.3 Continuous OAE deployments

Alkalinity is released at each site using continuous and pulse release protocols. For continuous OAE experiments, a constant Alk flux f_A is applied to the ECCO-Darwin surface-ocean layer (which is 10 m thick) over a regionally-defined deployment site from January 1995 to December 2017. Continuous experiments are performed for all five deployment sites described in Section 2.2.2.

Experiment Name	Abbreviation	${f Regional}$	Deployment Area	Experiment Type	Potential DIC	$mCDR_{pot}$: Mean/Range
		Bounds	$ imes 10^3 ~ {f km}^2$		Removed	(mol C/mol Alk)
North Atlantic	NAS	$16^{\circ}W$ -23°W	270	Continuous	$10^{-2} \ {\rm PgC \ yr^{-1}}$	0.854
Subduction		$56^{\circ}N-62^{\circ}N$		Monthly-pulse	$10^{-2} \ \mathrm{PgC}$	0.834 - 0.876
				Yearly-pulse	$12\times 10^{-2}~{\rm PgC}$	
Western Boundary	WBC	$144^{\circ}\mathrm{E}{-}148^{\circ}\mathrm{E}$	267	Continuous	$10^{-2}~{\rm PgC~yr^{-1}}$	0.807
Current		$31^{\circ}N$ - $38^{\circ}N$				0.792 - 0.826
Antarctic Circumpolar	ACC	$3^{\circ}\mathrm{E-}3^{\circ}\mathrm{W}$	268	Continuous	$10^{-2}~{ m PgC}~{ m yr}^{-1}$	0.876
Current		$45^\circ\mathrm{S}{-50}^\circ\mathrm{S}$		Monthly-pulse	$10^{-2} \ \mathrm{PgC}$	0.866 - 0.899
				Yearly-pulse	$12\times 10^{-2}~{\rm PgC}$	
Equatorial Upwelling	EU	$165^{\circ}W{-}170^{\circ}W$	267	Continuous	$10^{-2} \ {\rm PgC} \ {\rm yr}^{-1}$	0.799
		$2^{\circ}S-2^{\circ}N$				0.783 - 0.811
Subtropical Gyre	STG	$130^{\circ}\mathrm{W}{-}135^{\circ}\mathrm{W}$	266	Continuous	$10^{-2} \ {\rm PgC} \ {\rm yr}^{-1}$	0.834
		$30^{\circ}N^{-35_{\circ}N}$				0.822 - 0.844
Table 2. List of OAE e	xperiments: Experin	nent names and th	teir abbreviations used in	this work; regional bound	ds oand surface area	of deployment site;
experiment type with resp	ect to OAE injection	n duration; potent	ial DIC removed assumi	ng typical ocean conditio	ns (i.e., <i>DIC</i> _{tot,pot} fi	rom Eq. 6, assuming
$mCDR_{pot} = 0.8$; a	nd mean <i>mCDR</i> _{pot} o	over the deployme	nt site from ECCO-Darw	in (temporally-averaged \mathbf{v}	value over the simulz	ation period and minimum and
maximum monthly values). OAE deployment	sites are shown in	Figure 1.			

For each of these experiments, an area-integrated alkalinity flux $\int f_A dA = 3.33 \times$ 322 10^7 mol Alk s⁻¹ is applied over a horizontal area $A \approx 270 \times 10^3$ km² and characteris-323 tic length scale $\sqrt{A} \approx 500$ km. The amount of deployed Alk is such that each exper-324 iment has the potential to remove $\Delta DIC_{pot} = 10^{-2} \text{ Pg C yr}^{-1}$ from the atmosphere, 325 assuming that $mCDR_{pot} = 0.8$. In reality, $mCDR_{pot}$ is not 0.8 in all of the OAE deploy-326 ment regions. As discussed in Sec. 3.1, $mCDR_{pot}$ ranges from about 0.75 at the equa-327 tor to 0.9 at the poles, with 0.8 being a representative global-mean value. Additionally, 328 the true ΔDIC in each experiment will differ from the associated ΔDIC_{pot} due to ocean 329 dynamics. 330

The choice of a deployment area A and OAE flux f_A are somewhat arbitrary, and the results will depend on these choices. However, we expect the results to be fairly insensitive to modest reductions or increases in the area for these multi-decade experiments because 1) the ocean tends to mix material laterally over a large area on these timescales and 2) the model grid cells are nearly 100 km wide with no capability to treat subgridscale plume physics and chemistry. Furthermore, the results are expected to be relatively insensitive to modest adjustments of f_A .

We note that the magnitude of ocean net CO₂ uptake, pH perturbations, and other possible environmental impacts, which will be specific to the particular OAE approach used (and might include inorganic mineral precipitation and impact on marine food web via the introduction of micro-nutrients and trace metals), are expected to be strongly correlated with the magnitude of the OAE *Alk* flux. In this work, we do not explore these environmental impacts in depth, as they are specific to the particular OAE approach.

344

2.2.4 Pulse OAE deployments

For two deployment sites associated with strong seasonality in mCDR efficiency (NAS and ACC), we performed three additional "pulse" experiments with shorter Alkdeployments. Although the duration of the Alk pulse in these experiments may appear long, we stress that these timescales are fairly short compared to typical annual-to-multiannual timescales associated with OAE-attributed net CO₂ removal (He & Tyka, 2023).

For two monthly-pulse experiments, OAE is applied for a duration of 31 days, starting on January 1, 1995 and July 1, 1995; these monthly-pulse experiments are termed Jan1995 and Jul1995 experiments, respectively. The monthly-pulse experiments were chosen because they are perceived to be the months associated with approximately minimum and maximum $mCDR_{eff}$. For these experiments, the magnitude of the Alk flux is such that each of the pulse experiment has the potential to remove 10^{-2} Pg C from the atmosphere (assuming $mCDR_{pot} = 0.8$).

For the *yearly-pulse* OAE experiments, Alk is deployed during a single year (from January 1st 1995 to December 31st 1995) and the magnitude of the Alk flux is equal to that of the monthly pulse experiments, so the potential CO₂ removed from the atmosphere is roughly 12 times larger than in each of the monthly-pulse experiments. We refer to these experiments as *Yr1995* experiments.

362

2.2.5 Efficiency of pulse OAE estimated from continuous experiment

In this study, we focus primarily on continuous OAE deployments, as they allow 363 us to extract expanded insights into mCDR efficiency from each simulation compared 364 to single pulse experiments. As shown in Zhou et al. (2025) and further demonstrated 365 in our results, mCDR efficiencies derived from pulse experiments exhibit substantial sen-366 sitivity to the deployment month, often persisting more than a decade after the pertur-367 bation. Moreover, as discussed in Sec. 3.3.2, we demonstrate that a representative mCDR 368 efficiency for an ensemble of pulse experiments, initiated across different months, can be 369 effectively estimated using output from the continuous experiments and the derived met-370 ric $mCDR_{eff}^p$. Here we describe and schematically illustrate the relationship between pulse 371 experiments and continuous experiments using Fig. 2. 372

We first consider a pulse experiment deployed over a surface-ocean area A_d instan-373 taneously at time t = 0 (Fig. 2a). The net CO₂ exchange evolves on monthly to multi-374 annual timescales, superimposed on the background circulation-driven transport of OAE-375 modified waters. In Fig. 2a, a trajectory of OAE-modified waters and the correspond-376 ing values of δDIC_{tot} are shown at multiple equidistant time intervals after start of the 377 deployment (δDIC_{tot} is the incremental increase in ocean DIC_{tot} or the net CO₂ flux 378 integrated over the OAE-impacted area during one time increment Δt). The value of η 379 at time $t = n\Delta t$ is calculated by summing the product of $\Delta t \cdot \delta DIC_{tot}$ over all time 380 increments along the trajectory of OAE-perturbed waters (i.e., over Δt , $2\Delta t$, ..., $n\Delta t$) 381 and normalizing by the product of $\Delta t \cdot \Delta Alk_{tot}$ (see Eq. 2). The value of $mCDR_{eff}$ is 382 computed by normalizing η with the $mCDR_{pot}$ at the time of deployment (Eq. 7). 383

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We next consider a continuous OAE experiment deployed over the same surface-384 ocean area A_d , starting at time t = 0 (Fig. 2b). This continuous deployment can be 385 conceptualized as a series of n instantaneous incremental deployments, with each incre-386 ment injecting $\delta Alk_{tot} = \Delta Alk_{tot}/n$ over successive time intervals Δt , $2\Delta t$, ..., $n\Delta t$. 387 The value of $mCDR_{eff}^p$ at time $n\Delta t$, where n is the total number of time increments in 388 the deployment, is calculated by summing δDIC_{tot} from each incremental deployment 389 at time $n\Delta t$, normalized by the product of δAlk_{tot} and $mCDR_{pot}$ (Eq. 9). For the first 390 pulse, normalized δDIC_{tot} is evaluated at time $n\Delta t$ after deployment, for the second in-391 crement at time $(n-1)\Delta t$, and for the last increment at time Δt after deployment. This 392 summation accounts for multiple deployment trajectories (each corresponding to the space-393 time evolution of one of the incremental deployments), covering the time interval from 394 0 to $n\Delta t$ — this is similar to a summation of the net CO₂ flux for the pulse experiment. 395

In summary, $mCDR_{eff}$ time integrated in a pulse experiment is akin to integration 396 of normalized net CO_2 flux along a single deployment trajectory, while $mCDR_{eff}^p$ is in-397 tegrated across multiple incremental deployment trajectories. For an idealized steady-398 state ocean we expect the two quantities to be exactly equal. However, since the real ocean 399 is far from steady-state, due to seasonal and interannual variability for example, $mCDR_{eff}^p$ 400 represents $mCDR_{eff}$ as derived from an ensemble of back-to-back pulse experiments, each 401 initialized to capture the variability across a representative range of space-time-evolving 402 ocean conditions. 403

404

2.3 ECCO-Darwin Description

The ECCO-Darwin model and data assimilation methods have been extensively 405 described in the literature (e.g., Brix et al., 2015; Manizza et al., 2019, 2023; Carroll et 406 al., 2020, 2022; Bertin et al., 2023). In particular, a technical description of the ECCO-407 Darwin model set-up, observational constraints, and optimization methodology is pre-408 sented in Carroll et al. (2020). In this study, we use a coarser-resolution (1° vs. $1/3^{\circ}$ hor-409 izontal grid spacing) version of the Carroll et al. (2020) solution. Below, we provide a 410 brief introduction to ECCO-Darwin and highlight the unique features of this model that 411 are essential for our OAE studies. 412

The Lat-Lon-Cap-90 (LLC90) version of ECCO-Darwin used in this paper has 1° nominal horizontal grid spacing, spans 1992–2017, and is based on ocean circulation and



Figure 2. Schematic representing (a) a pulse OAE deployment and (b) continuous OAE deployment. Dark blue boxes represent the OAE injection area and light blue boxes represent trajectories of OAE-impacted waters across space and time; yellow arrows indicate net CO₂ up-take. δDIC and δAlk are the DIC increase due to net CO₂ flux and Alk deployment over time increment Δt .

physical tracers (i.e., temperature, salinity, and sea ice) from the Estimating the Circu-415 lation and Climate of the Ocean (ECCO) Version 4 release 4 solution (V4r4; ECCO Con-416 sortium et al., 2021; Forget, Campin, et al., 2015). Horizontal grid spacing varies from 417 110 km at mid-latitudes to roughly 42 km at high latitudes. The vertical grid spacing 418 increases from 10 m near the surface to 457 m near the seafloor. Since the horizontal dis-419 cretization is insufficient to resolve mesoscale eddies, their impact on large-scale ocean 420 circulation is parameterized using the Redi (1982) and Gent and McWilliams (1990) schemes; 421 vertical mixing is parameterized with the Gaspar et al. (1990) scheme. 422

The ECCO V4r4 circulation estimate is used at each time step to drive an online 423 biogeochemistry and ecosystem model developed by the Massachusetts Institute of Tech-424 nology Darwin Project (Follows et al., 2007; Dutkiewicz et al., 2015, 2020). In this ver-425 sion of the model, the Darwin model does not feedback on the ECCO circulation. The 426 Darwin model includes the cycling of organic and inorganic carbon, phosphorus, iron, 427 silica, oxygen, and alkalinity. Carbonate chemistry is based on the efficient solver of Follows 428 et al. (2006). Air-sea CO₂ flux is computed using the parameterization of Wanninkhof 429 (1992) and forced with atmospheric partial pressure of CO_2 from the zonally-averaged 430 National Oceanic and Atmospheric Administration Marine Boundary Layer Reference 431 (NOAA MBL) product (Andrews et al., 2014). The Darwin ecology includes five large-432 to-small phytoplankton functional types (diatoms, other large eukaryotes, Synechococ-433 cus, and low- and high-light adapted Prochlorococcus), along with two zooplankton types 434 that graze preferentially on either large eukaryotes or small picoplankton. 435

Physical observations are assimilated using the adjoint method (i.e., 4-D-Var; Wun-436 sch et al., 2009; Wunsch & Heimbach, 2013), which minimizes a weighted least squares 437 sum of model-data misfit (i.e., a cost function) to optimize initial conditions; time-varying 438 surface-ocean boundary conditions; and time-invariant, three-dimensional mixing coef-439 ficients for along-isopycnal, cross-isopycnal, and isopycnal thickness diffusivity. Because 440 the initial conditions, surface boundary conditions, and mixing coefficients are estimated 441 as part of the adjoint-method optimization, the ECCO ocean circulation estimate has 442 negligible drift and therefore does not require spin-up. The biogeochemical model is op-443 timized in an additional step from the circulation using a low-dimensional Green's Funcллл tions approach (Menemenlis et al., 2005) to assimilate a variety of biogeochemical ob-445 servations and adjust Darwin initial conditions and ecological parameters. We neglect 446 the first 3 years of model simulation due to biogeochemical spin-up. The LLC90 ECCO-447

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Darwin version closely matches the previously-published solution (Supporting Informa-tion Fig. S4).

450

2.4 Rapid-mCDR: 1D model for mCDR simulations

At the present time, the ECCO-Darwin simulations discussed in the previous section might be computationally too expensive for simulating and quantifying OAE efficiency, especially if a large number of OAE deployment sites and seasons are considered. To provide a numerically-efficient approach and isolate and elucidate interactions between OAE and vertical transport processes, we next develop a 1D model *rapid-mCDR* which simulates the tight coupling between OAE-modified *Alk* and *DIC* and solves for conservation equations for these quantities in Eulerian form:

$$\frac{\partial}{\partial t}\Delta\widehat{Alk} = -\frac{\partial}{\partial z}\left(\overline{w}^*\Delta\widehat{Alk}\right) + \frac{\partial}{\partial z}\left(\overline{K}^*\frac{\partial}{\partial z}\Delta\widehat{Alk}\right) + \frac{\delta_{z_k,0}}{\Delta z_1}\widehat{f_{Alk}},\tag{10}$$

$$\frac{\partial}{\partial t}\Delta\widehat{DIC} = -\frac{\partial}{\partial z}\left(\overline{w}^*\Delta\widehat{DIC}\right) + \frac{\partial}{\partial z}\left(\overline{K}^*\frac{\partial}{\partial z}\Delta\widehat{DIC}\right) - \frac{\delta_{z_k,0}}{\Delta z_1}\Delta\widehat{f_C}, \text{and}$$
(11)

$$\Delta \widehat{f_C} = \overline{\kappa}^* (1 - \overline{a}_{ice}^*) \left(\frac{\overline{\partial p \text{CO}_2^{aq}}^*}{\partial Alk} \Delta \widehat{Alk} + \frac{\overline{\partial p \text{CO}_2^{aq}}^*}{\partial DIC} \Delta \widehat{DIC} \right), \tag{12}$$

where ΔDIC , ΔAlk represent OAE perturbations of DIC and Alk concentrations, and 458 Δf_C is the net CO₂ flux from the OAE-perturbed simulation with respect to the base-459 line simulation. Variables w and K are 3D vertical velocity and diffusivity, κ is the pis-460 ton velocity, and a_{ice} is sea-ice cover — all these variables are taken from the baseline 461 simulation, as they are not modified by OAE in our experiments. $\hat{\varphi}$ and $\overline{\varphi}^*$ represent horizontally-462 integrated values of φ over the global ocean and horizontally-averaged values of rapid-463 mCDR forcing φ over the OAE-impacted area, respectively. The value of $\delta_{z_k,0}$ is 1 for 464 the uppermost rapid-mCDR vertical level and zero otherwise, and Δz_1 represents the 465 ocean depth represented by that layer. 466

Eqs. 10 and 11 relate the time derivative of $\Delta \widehat{Alk}$ and $\Delta \widehat{DIC}$ (terms on the left hand side of these two equations) to the vertical advection and diffusion terms (first and second term on the right hand side of these equations) and prescribed Alk deployment rate or OAE-attributed net CO₂ uptake (the last terms in Equations 10 and 11, respectively). These two equations are derived by simplifying ECCO-Darwin budget equations

(Supporting Information Text S3), guided by analysis of the budget terms in the five regionalscale OAE experiments (Supporting Information Figs. S5-S6). The following two approx-473 imations are used: 1) the biological source term is neglected and 2) the products of ver-474 tical velocity and Alk perturbations are linearized as: $w\widehat{\Delta Alk} \approx \overline{w}^* \Delta \widehat{Alk}$. This approx-475 imation neglects correlation between the vertical velocity and ΔAlk over the OAE-impacted 476 regions. A similar approximation is made for *DIC* and diffusion terms in the conserva-477 tion equation. 478

472

Eq. 12 represents the horizontally-integrated net CO_2 flux due to OAE, which is 479 a function of ocean-surface perturbations $\Delta \widehat{Alk}$ and $\Delta \widehat{DIC}$ and $p \operatorname{CO}_2^{aq}$ sensitivities. The 480 $p CO_2^{aq}$ sensitivities were estimated from the surface-ocean conditions in the baseline sim-481 ulation using PyCO2SYS. The rapid-mCDR equations are solved for 50 vertical levels 482 (which coincide with the ECCO-Darwin vertical levels) using a 1-day time step. The nu-483 merical finite difference scheme uses an implicit Euler method for time derivatives, which 484 ensures numerical stability. A simple numerical stability analysis and sensitivity study 485 indicates that the daily time step is sufficient (not shown). At the ocean floor, we as-486 sume net zero flux of $\Delta \widehat{Alk}$, $\Delta \widehat{DIC}$, which is used as a bottom boundary condition for 487 Eqs. 10-11. We initialize rapid-mCDR at January 1, 1995 (before the start of OAE de-488 ployments), at which time the Alk and DIC perturbations are set to zero. Rapid-mCDR 489 is then integrated through the ECCO-Darwin period (January 1st, 1995 to December 490 31st, 2017). 491

We note that rapid-mCDR is a 1D model that simulates vertical processes only, 492 and therefore it does not explicitly represent the impact of horizontal transport (advec-493 tion and diffusion) on OAE. Horizontal transport can however be implicitly represented 494 by providing the required inputs for rapid-mCDR ($\overline{w}^*, \overline{K}^*$ and pCO_2^{aq} sensitivities in 495 Equation 12) following the deployment trajectory (i.e., the space-time evolution of the 496 OAE perturbation), which essentially "transports" the rapid-mCDR vertical column along 497 that trajectory. In this work, rapid-mCDR inputs are taken as the spatially-averaged val-498 ues over OAE-impacted regions that are defined using two distinct averaging approaches: 499

• *DeployAvg*: This is the simplest approach, which neglects all horizontal transport. 500 Here rapid-mCDR inputs are averaged horizontally over the deployment site only. 501 In this method, all OAE and DIC perturbations, as well as CO_2 uptake, are com-502 puted at the deployment site. This approach is therefore appropriate for deploy-503

- ment sites with relatively weak horizontal transport. Results from rapid-mCDR 504 using this method are referred to as "rapid-mCDR(DeployAve)". 505 • TransportAvg: This approach accounts for the space-time horizontal advection and 506 diffusion of the rapid-mCDR water column — which is driven by surface-ocean 507 currents. In this method, ocean conditions are computed as an area-weighted mean 508 over the region where OAE modifies surface pCO_2^{aq} , with the weights being pro-509 portional to $\Delta p CO_2^{aq}$. Results from rapid-mCDR using this approach are referred 510 to as "rapid-mCDR(TransAve)". 511
- 512

3 ECCO-Darwin results

513

3.1 mCDR Potential

Figure 3 shows global-ocean time-mean $mCDR_{pot}$ and its climatological seasonal 514 cycle from the ECCO-Darwin and OceanSODA-ETHZ. Time-mean $mCDR_{pot}$ reveals a 515 pronounced meridional gradient, with the lowest values (approximately 0.75 mol C/mol Alk) 516 located in the tropics, progressively increasing poleward and eventually exceeding 0.9 mol C/mol Alk 517 (Fig. 3a). For the same latitudinal range, values in regions dominated by western bound-518 ary currents tend to be lower than eastern boundary currents. The amplitude of the sea-519 sonal cycle of $mCDR_{pot}$ is below 0.1 mol C/mol Alk throughout the global ocean (Fig-520 ure 3b) and less than 0.05 mol C/mol Alk at the five deployment sites (Table 2). The 521 most pronounced seasonal cycle occurs in northern mid-latitudes and polar regions, where 522 the highest values are found in western boundary current regions, such as the Gulf Stream 523 and Kuroshio extensions and the Brazil-Malvinas Confluence. Across the chosen five de-524 ployment sites, average $mCDR_{pot}$ from ECCO-Darwin ranges from 0.799 mol C/mol Alk 525 (EU) to $0.854 \mod C/mol Alk$ (NAS) (Table 2). 526

Following Takahashi et al. (1993), we can understand the reasons and attributes 527 of the variability of $mCDR_{pot}$ by recognizing that its value is the negative product of DIC/Alk528 and $\gamma_{Alk}/\gamma_{DIC}$ (Eq. 5). The value of γ_{DIC} (the buffer or Revelle Factor) ranges from 529 about 8 at the equator to 14 at the poles and γ_{Alk} ranges from roughly -7.4 to -13.3 (e.g. 530 Sarmiento & Gruber, 2006), while their ratio varies comparatively little over the global 531 ocean and seasons. Therefore, the variability of $mCDR_{pot}$ is primarily controlled by the 532 variability of the DIC/Alk ratio, which ranges from about 0.83 at the equator to 0.94 533 at the poles. Due to the strong correlation between surface-ocean Alk and salinity, the 534

-22-



Figure 3. $mCDR_{pot}$ from the baseline ECCO-Darwin simulation (left) and OceanSODA-ETHZ dataset (right) showing (a) time-mean values over the ECCO-Darwin period (January 1995 to December 2017) and (b) magnitude of climatological seasonal cycle.

variations of surface-ocean DIC/Alk are very similar to the variations of salinity-normalized

DIC and are similarly controlled by the processes other than evaporation and precip-

itation that affect *DIC*: ocean transport (circulation and mixing), biology, and air-sea

⁵³⁸ flux (Takahashi et al., 1993, 2014; Gregor & Gruber, 2021).

The meridional gradient of DIC/Alk, and hence $mCDR_{pot}$, is thought to be caused 539 by two main factors: the meridional gradient of solar heating and SST, which tends to 540 increase surface-ocean pCO_2^{aq} and hence carbon outgassing at low latitudes (all else equal), 541 as well as upwelling and entrainment of Alk- and DIC-rich waters at subpolar latitudes, 542 which tend to enhance *DIC* in iron-limited regimes where biological productivity is re-543 duced (Wu et al., 2019). The seasonal variations of $mCDR_{pot}$ are driven by a compli-544 cated variety of different combinations of air-sea CO₂ flux, ocean transport, and biol-545 ogy, with the latter often playing a leading role in the seasonal cycle in mid- to high-latitudes 546 (Sarmiento & Gruber, 2006). See Carroll et al. (2022) for a recent global description of 547 DIC dynamics derived from ECCO-Darwin. 548

Time-mean $mCDR_{pot}$ computed from both datasets exhibit similar features, with 549 model-data differences generally not exceeding 0.025 mol C/mol Alk. One notable dis-550 tinction is that OceanSODA-ETHZ values are marginally lower in eastern subtropical 551 basins. Although both ECCO-Darwin and OceanSODA-ETHZ exhibit similar seasonal 552 patterns of $mCDR_{pot}$, the seasonal cycles in OceanSODA-ETHZ tend to have larger mag-553 nitudes. Nevertheless, both ECCO-Darwin and OceanSODA-ETHZ demonstrate sim-554 ilar structure in $mCDR_{pot}$ suggesting it is relatively accurate in both and justifying our 555 use of ECCO-Darwin to quantify mCDR efficiency. 556

In summary, the most effective OAE deployments, based solely on their potential to remove atmospheric CO₂ would be over polar oceans, provided the OAE-impacted waters were maintained at their simulated conditions throughout re-equilibration. However, in the next sections, when we consider ocean dynamics that are captured by the dynamical efficiency factor ($mCDR_{eff}$), this narrative substantially changes.

562

3.2 OAE impact on ocean state for continuous OAE experiments

Before quantifying OAE efficiency, we first investigate the impact of OAE on the ocean state for the five continuous experiments. These results serve as an illustration only, because the environmental impacts are expected to scale with the magnitude of deployed Alk. We examine the spatial patterns of atmospheric CO₂ uptake and alteration of surfaceocean pH, as well as how OAE-impacted seawater mixes and subducts in the ocean interior.

569	For the five continuous OAE experiments, Figure 4 shows a map of time-integrated
570	net CO ₂ uptake due to OAE from the end of the ECCO-Darwin period (i.e. $\int \Delta f_c \mathrm{d}t$
571	integrated from the January 1, 1995 to December 31, 2017). For all OAE deployments,
572	the time-integrated net $\rm CO_2$ flux is largest close to the deployment site and its footprint
573	is indicative of near-surface horizontal advection, with the following key features:
574	• For NAS, the North Atlantic and the Norwegian Currents transport OAE-modified
575	waters towards high-latitude regions, with the flow bifurcating near Iceland. As
576	a result, the largest values of net $\rm CO_2$ flux are found at, or north of the deploy-
577	ment site.
578	- For WBC and ACC, predominant zonal transport results in the largest net CO_2
579	flux values located primarily east of the deployment sites. In particular, the strong
580	Antarctic Circumpolar Current in ACC spreads the net CO_2 flux eastward over
581	a large region of the Southern Ocean.
582	• For EU, equatorial upwelling and upper-ocean zonal flow both north and south
583	of the equator spread the net CO_2 flux footprint over most of the tropical/subtropical
584	Pacific Ocean. The signature of cumulative net CO_2 flux for EU covers the largest
585	horizontal area (not shown), while the maximum magnitude is the lowest of all
586	5 experiments.
587	• For STG, the anticyclonic circulation associated with the subtropical gyre advects
588	OAE-impacted waters towards the southwest, spreading the net $\rm CO_2$ flux foot-
589	print west of Southern California and Baja Mexico.
590	To illustrate the depth of the OAE perturbation across the five continuous OAE
591	experiments, Supporting Information, Figure S8b shows the temporal evolution of the
592	depth above which 95% of the deployed Alk remains. We adopt this depth threshold as
593	a metric to demarcate OAE-modified waters from those unaffected by OAE. For all OAE
594	experiments, the OAE perturbation spreads to deeper waters with elapsed time after de-

- ⁵⁹⁵ ployment, with large differences occurring in the OAE perturbation depth across all ex-
- $_{596}$ periments. By the end of the simulation, the *Alk* perturbation reaches depths in excess
- of 2000 m in NAS and roughly 800 m in ACC. For the other three experiments, Alk per-



All Experiments

Figure 4. Time-integrated net CO_2 flux due to OAE from January 1995 to December 2017 for the 5 continuous OAE experiments. The color scale is logarithmic, highlighting variations in CO_2 uptake intensity. Isolines represent *DIC* increases of 0.1, 1, 5, 10, and 50 mol C m⁻². Black boxes show OAE deployment sites. Upper panel shows all 5 OAE experiments across the global ocean; lower panels show individual OAE experiments.

turbations remain much closer to the ocean surface and depths below roughly 500 m remain largely unaffected.

In Supporting Information Text S3 (and Figures S5 - S6) we also discuss horizontally-600 integrated budgets for *DIC* and *Alk* perturbations for the five continuous OAE exper-601 iments. These budgets separate and quantify the contributions of key processes that mod-602 ify DIC and Alk perturbations. With the exception of the air-sea interface, where the 603 DIC and Alk perturbations increase due to net CO_2 flux from the atmosphere and the 604 prescribed Alk flux, respectively, changes to DIC and Alk perturbations are predom-605 inantly dominated by vertical ocean dynamics, while the contribution of biology is neg-606 ligible. 607

Across all deployment sites, excluding EU, a pronounced seasonality characterizes 608 the strength of vertical mixing and advection, coinciding with variations in mixed layer 609 depth (MLD; Supporting Information, Figures S5 - S6). As the MLD deepens, DIC and 610 Alk perturbations are transported into deeper waters, potentially sequestering them from 611 the atmosphere (which inhibits or delays net CO_2 uptake) until the MLD shoals again. 612 Notably, the relative influence of vertical advection and diffusivity (i.e., mixing) varies 613 significantly by deployment site. The MLD and its seasonal variability differ substan-614 tially among sites, with NAS having the deepest seasonal MLD. 615

616

3.3 Efficiency of alkalinity enhancement

617

3.3.1 Continuous OAE experiments

For the five continuous OAE experiments, Figs. 5 and 6 show key aspects associ-618 ated with net CO₂ uptake. Time series showing the total amount of deployed Alk (ΔAlk_{tot}) 619 and potential *DIC* uptake and realized net *DIC* uptake ($\Delta DIC_{tot,pot}$ and ΔDIC_{tot} , re-620 spectively) are shown on Fig. 5. In Fig 6a, we show $mCDR_{eff}$, computed from the start 621 of the OAE deployment (i.e., January 1, 1995) to the time shown on the x-axis. Fig. 6b 622 shows $mCDR_{eff}^{p}$ filtered with a centered 1-year running-mean filter. The running-mean 623 filter is applied to remove the large seasonal cycle of net CO₂ uptake. Fig. 6c shows the 624 time-mean seasonal cycle of $mCDR_{eff}^p$ over the last ten years of simulation. In Support-625 ing Information (Fig. S7) we show the time series of horizontally-averaged profiles of $mCDR_{equil}$. 626 The deployment locations associated with large seasonality are likely related to high sea-627 sonal dependence of pulse mCDR efficiency, which we further investigate in Section 3.3.2. 628



Figure 5. Continuous OAE experiment initiated on January 1, 1995. Time series of ΔAlk_{tot} (black line), ΔDIC_{tot} (solid color lines), $\Delta DIC_{tot,pot}$ (dashed colored lines). The colors represent the five different OAE deployments, as indicated by the legend.

629	From the perspective of potential for net CO_2 removal, the deployment locations
630	closer to the polar regions are associated with the highest values (i.e., the highest $\Delta DIC_{tot,pot}$
631	in Fig. 5) as already discussed above. However, the actual net CO_2 removal (ΔDIC_{tot})
632	is additionally modified by the dynamical efficiency, which varies substantially among
633	the deployment sites (Fig. 5). In all cases, ΔDIC_{tot} is considerably lower than ΔDIC_{pot}
634	throughout the 23-year experiment, which is longer than the the air-sea adjustment timescale,
635	indicating a strong control of ocean dynamical processes on net $\rm CO_2$ removal. Fig. 5 also
636	shows that the variability between sites in terms of $DIC_{tot,pot}$ is smaller than that of DIC_{tot} ,
637	emphasizing the critical role that variations in ocean dynamics play in driving differences
638	in OAE efficiency across the sites.

For all continuous experiments, the dynamical efficiency $(mCDR_{eff})$ curves (Fig. 6a) increase nonlinearly with time after deployment, exhibiting the following key characteristics:

- ACC is associated with the most-rapid increase of $mCDR_{eff}$, where values exceed 0.75 within 5 years after the start of OAE and also reach one of the highest values by the end of the simulation (0.91). This is consistent with this site having the most rapid increase of $mCDR_{equil}$ in the upper ocean, as shown in Supporting Information (Fig. S7).
- For all deployments, EU is associated with the slowest initial increase of $mCDR_{eff}$, consistent with the slowest increase of $mCDR_{equil}$. However, after roughly 13 years after deployment its values reach that of the ACC and by the end of the simula-



Figure 6. Continuous OAE experiment initiated on January 1, 1995 (a) Time series of dynamical mCDR efficiency; (b) Centered 1-year running-mean values of $mCDR_{eff}^p$; (c) Average seasonal cycle of $mCDR_{eff}^p$ over the last simulation decade. The colors represent the five different OAE deployments, as indicated by the legend.

tion $mCDR_{eff}$ in this region yield the highest value of all simulations, 0.95. $mCDR_{eff}$ in this region diverges from the typical shape due to strong interannual variability, which we discuss below. • For the other three experiments (STG, WBC, and NAS), $mCDR_{eff}$ behaves remarkably similar over the first decade after deployment — by the end of 2017 their values differ by only a few percent each (0.84, 0.81, and 0.77 for STG, WBC, and NAS, respectively), despite considerable differences in the ocean dynamics of these

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sites.

Next we discuss the behaviour of $mCDR_{eff}^p$, as this represents the overall efficiency 658 of the pulse experiment for the corresponding site. $mCDR_{eff}^{p}$ exhibits nonlinear behav-659 ior (6b) similar to that of $mCDR_{eff}$, but also highlights interannual variability. Note that 660 for most of the experiments, $mCDR_{eff}^p$ is also associated with strong seasonality (Fig-661 ure 6c), which is filtered from the timeseries shown on Figure 6b. EU exhibits the largest 662 interannual variability in $mCDR_{eff}^p$, superimposed on the tapered nonlinear and nearly 663 monotonic increase. This interannual variability is positively correlated with the mul-664 tivariate El-Niño/Southern Oscillation (ENSO) index (Wolter & Timlin, 2011, not shown), 665 indicating that ENSO can have a substantial impact on net CO_2 uptake in the Tropi-666 cal Pacific Ocean. We note that other locations also exhibit interannual variability in 667 $mCDR_{eff}^p$, albeit weaker than in EU. The values of running-mean $mCDR_{eff}^p$ in Fig. 6b 668 can exceed one for a limited time period, which is most evident for the EU experiment. 669 This does not mean that dynamical OAE efficiency exceeds 100%, rather it reflects tran-670 sient mismatches in time between net CO_2 uptake and injected Alk flux, which are driven 671 by ocean-atmosphere dynamics. 672

Figure 6c shows that $mCDR_{eff}^p$ for NAS and WBC, and to some extent ACC, are associated with a strong seasonally-dependent response of $mCDR_{eff}^p$ to the constant *Alk* flux, yielding maximum values (and thus strongest net CO₂ uptake) in winter and minimum values in summer. Peak monthly values differ from the annual-mean values by up to 40%. In ACC, the magnitude of the seasonal cycle of $mCDR_{eff}^p$ is roughly half that of NAS and is shifted in phase roughly 6 months, due to its location in the southern hemisphere.

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3.3.2 Pulse OAE experiments

To understand how $mCDR_{eff}$ varies seasonally as a function of deployment month, we use three targeted pulse OAE experiments for the NAS and ACC. Each experiment uses a different OAE deployment strategy, Yr1995 (year-long pulse during 1995), Jan1995 (pulse in January 1995 only), and Jul1995 (pulse in July 1995 only), to further elucidate how $mCDR_{eff}$ depends on the season of deployment. Figure 7 shows the time series of $mCDR_{eff}$ from the pulse experiments and $mCDR_{eff}^{p}$ from the continuous experiments conducted at the same site, with deployment starting on January 1st, 1995.

For the three NAS experiments, the time evolution of $mCDR_{eff}$ is highly dependent on the month of Alk deployment (Figure 7a). By the end of simulation, Alk deployed in summer (Jul1995) reaches an efficiency of roughly 0.9 while the winter deployment (Jan1995) is only slightly above 0.6; the efficiency of the annual deployment (Yr1995) lies between these two extremes. Note that the seasonality in $mCDR_{eff}^p$ shown in Fig. 6 does not coincide with seasonality of $mCDR_{eff}$ for the pulse experiment.

For the NAS experiment, $mCDR_{eff}^{p}$ somewhat overestimates $mCDR_{eff}$ for the Yr1995 694 experiment, but it generally falls well between the values for Jan1995 and Jul1995 de-695 ployments, indicating that continuous virtual experiments can be used to characterize 696 the average dynamical efficiency of an ensemble of pulse deployments distributed evenly 697 throughout the seasonal cycle at this site. For the ACC experiments, seasonal variabil-698 ity in $mCDR_{eff}$ is evident during the initial years post-deployment, but after approxi-699 mately ten years all experiments achieve nearly maximal dynamical efficiency (Figure 7b). 700 Overall, the results at two sites in Figure 7 are suggestive that $mCDR_{eff}^{p}$ may be a rea-701 sonable approximation of the ensemble-average efficiency of pulse deployments. 702

We emphasize that the seasonality of $mCDR_{eff}^{p}$, which is discussed in Sec. 3.3.1, is likely related to, yet distinct from, the seasonality of $mCDR_{eff}$ observed in the pulse experiments. The first quantifies the seasonally-dependent response of net CO₂ flux to constant *Alk* forcing and the latter quantifies the response of net CO₂ flux to seasonallydependent *Alk* injection.

⁷⁰⁸ 4 Rapid-mCDR results

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In this section, we first compare the two versions of rapid-mCDR against ECCO-Darwin and discuss the difference in results when using the two spatial averaging meth-

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Figure 7. $mCDR_{eff}$ for monthly-pulse experiments (blue and red lines) and yearly-pulse experiments (black lines) and $mCDR_{eff}^p$ for continuous experiment shown as centered 1-year running-mean values (black dashed line); (a) NAS and (b) ACC.

ods to approximate the impact of horizontal transport described in Section 2.4. Then
as an example use case, we use rapid-mCDR to understand how and why mCDR efficiency varies latitudinally across a meridional section of the central Pacific Ocean.

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4.1 Evaluation of rapid-mCDR against ECCO-Darwin for the 5 OAE deployments

Figure 8 evaluates $mCDR_{eff}^{p}$ from rapid-mCDR simulations against ECCO-Darwin across all five continuous OAE experiments. As discussed in Sec. 2.4, we expect rapidmCDR(TransAve) to better reproduce ECCO-Darwin than rapid-mCDR(DeployAve) due to its more accurate representation of horizontal transport. Although the primary output of rapid-mCDR is net CO₂ uptake, here we show different aspects of $mCDR_{eff}^{p}$, including:

- 1. Scatter plots of monthly-mean $mCDR_{eff}^{p}$ from ECCO-Darwin and the two rapidmCDR versions. These provide a measure of the overall skill of rapid-mCDR in emulating CO₂ uptake efficiency (left panel).
- 2. Time series of $mCDR_{eff}^p$ using a 1-year centered-running mean, showing the bias in rapid-mCDR simulations (middle panel).

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3. Seasonal cycle of $mCDR_{eff}^p$, further indicating the skill of rapid-mCDR and seasonal bias (right panel).

⁷²⁹ Supporting Information Fig. S7 illustrates the agreement in $mCDR_{equil}$ between ⁷³⁰ ECCO-Darwin and the two rapid-mCDR versions, highlighting the consistent vertical ⁷³¹ Alk and DIC transport between the two models.

For NAS, the $mCDR_{eff}^{p}$ from rapid-mCDR(TransAve) agrees well with ECCO-Darwin 732 for the entire duration of the experiment (Fig. 8a). The coefficient of determination for 733 the monthly-mean values of $mCDR_{eff}^p$ is $R^2 = 0.9$. The rapid-mCDR(TransAve) slightly 734 underestimates annual-mean values of $mCDR_{eff}^p$ during the first part of the simulation, 735 but this underestimation is less than 0.05. The seasonal cycle of $mCDR_{eff}^p$ is well sim-736 ulated by this version of rapid-mCDR. The rapid-mCDR(DeployAve) somewhat over-737 estimates $mCDR_{eff}^p$ during most of the simulation period, except for the first five years 738 after the start of deployment (Fig. 8a). While this overestimation is primarily due to the 739 winter months, as revealed by comparison of the seasonal cycle, the overestimation re-740

mains present to some degree throughout the year. The winter overestimation is likely 741 dominated by the absence of sea ice for rapid-mCDR(DeployAve), which impacts both 742 ECCO-Darwin and rapid-mCDR(TransAve). The spatial average of sea-ice area over the 743 impacted region in ECCO-Darwin can reach up to 0.15 in the winter period (not shown), 744 which is expected to reduce winter CO_2 uptake (and therefore $mCDR_{eff}^p$) by roughly that 745 fraction. Despite the degradation in the rapid mCDR solution due to ignoring horizon-746 tal transport in rapid-mCDR (DeployAve), the coefficient of determination $R^2 = 0.67$ 747 and the time-mean bias are relatively modest. 748

For WBC, both versions of rapid-mCDR closely represent ECCO-Darwin, with only 749 a modest overestimation of the annual-mean values of $mCDR_{eff}^p$, and rapid-mCDR(TransAve) 750 providing a somewhat better match to ECCO-Darwin (Fig. 8b). This agreement holds 751 for both the time series of annual-mean values and the coefficients of determination, which 752 are $R^2 = 0.90$ for rapid-mCDR(TransAve) and $R^2 = 0.76$ for rapid-mCDR(DeployAve). 753 Furthermore, the seasonal cycles from both rapid-mCDR versions generally align well 754 with that of ECCO-Darwin. A similar level of performance or rapid-mCDR is observed 755 for ACC, as shown in Fig.8c. 756

For EU, the agreement of $mCDR_{eff}^p$ between ECCO-Darwin and the two rapid-mCDR 757 simulations is the poorest of all five OAE experiments, with $R^2 = 0.74$ for rapid-mCDR(TransAve) 758 and $R^2 = 0.03$ for rapid-mCDR(DeployAve) (Fig. 8d). The annual-mean comparison 759 shows that rapid-mCDR(DeployAve) is unable to sufficiently represent interannual vari-760 ability, which is large in this location. rapid-mCDR(TransAve) represents this interan-761 nual variability better, likely due to the fact that it approximates horizontal transport 762 and thus the dispersal of OAE-impacted waters better. Nevertheless, the mean bias av-763 eraged over the seasonal and interannual variability is relatively modest for both approaches. 764

In STG, rapid-mCDR(DeployAve) significantly underestimates $mCDR_{eff}^{p}$ approximately a decade after the start of deployment, while rapid-mCDR(TransAve) agrees better with ECCO-Darwin ($R^{2} = 0.31$ and 0.88, respectively). The cause of this underestimation is likely similar to the EU deployment, where after a number of years OAEimpacted waters spread across a large region, which the rapid-mCDR(DeployAve) approach does not capture.

⁷⁷¹ In Figure 9 we demonstrate the ability of rapid-mCDR to represent mCDR effi-⁷⁷² ciency for the three pulse experiments for NAS and ACC, which were previously shown

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Figure 8. Comparison of $mCDR_{eff}^p$ from ECCO-Darwin and both versions of rapid-mCDR. Left panels (a–e) show monthly-mean ECCO-Darwin vs. rapid-mCDR, along with associated R^2 values. Middle panels show time series using a 1-year centered-running mean; right panels show monthly-mean values to provide a zoom-in period during the last 10 years of simulation. Blue and red lines represent rapid-mCDR(TransAve) and rapid-mCDR(DeployAve), respectively. Black line in middle and right panels shows ECCO-Darwin.



Figure 9. *mCDR_{eff}* for monthly-pulse and yearly-pulse experiments in (a) NAS and (b) ACC. Solid lines show ECCO-Darwin, dashed lines show rapid-mCDR(TransAve).

to strongly vary with deployment season. Here, only results from rapid-mCDR(TransAve) 773 are shown. For NAS, rapid-mCDR agrees well with ECCO-Darwin over the first five years 774 after deployment and shows some skill in representing seasonally-varying $mCDR_{eff}$, as 775 discussed above. However, by the end of the simulation rapid-mCDR somewhat over-776 estimates $mCDR_{eff}$; this overestimation is consistent for all three experiments. For ACC, 777 $mCDR_{eff}$ is overestimated by rapid-mCDR — a result that is consistent with the con-778 tinuous OAE experiments in this region. Rapid-mCDR predicts that by the end of the 779 simulation $mCDR_{eff}$ approaches a value of one, which is roughly 0.1 larger than ECCO-780 Darwin. Overall, despite its simplicity, rapid-mCDR generally reproduces the results of 781 ECCO-Darwin. 782

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4.2 Expanding rapid-mCDR to ocean-basin scales

In this section, we provide an example use case of rapid-mCDR to characterize dynamical mCDR efficiency ($mCDR_{eff}$) across space-time scales that might be prohibitively expensive to examine with ECCO-Darwin. We also use rapid-mCDR to isolate the physical processes (such as sea-ice cover or vertical mixing) that reduce $mCDR_{eff}$ by analyzing the model's response to modifications in the strength of these processes. This approach would be challenging with ECCO-Darwin, as altering the strength of such processes in the numerical ocean model could cause unintended downstream effects in the simulated fields.

We simulate Alk deployment across the meridional extent of the Pacific Ocean, cen-792 tered on 165° W, with deployments spaced 1° apart in latitude from 77° S to 52° N. This 793 latitudinal range is chosen so that each deployment represents open-ocean conditions. 794 Each deployment covers a rectangular area 10° in longitude by 3° in latitude; the cen-795 tral deployment locations are shown in Fig. 10a. For all of these deployments, we use 796 rapid-mCDR(DeployAve) where the inputs are taken from the baseline ECCO-Darwin 797 simulation. At each deployment location, we perform three experiments, corresponding 798 to the three ECCO-Darwin pulse experiments discussed in Section 2.2.4: Yr1995, Jul1995, 799 and Yr1995. As with ECCO-Darwin, these experiments are run until December 31, 2017 800 and the $mCDR_{eff}$ values are evaluated at the end of simulation (roughly 23 years after 801 deployment). 802

Furthermore, to isolate the effects of physical processes (vertical advection, vertical diffusivity, and sea-ice cover) on $mCDR_{eff}$, we performed three additional sets of sensitivity experiments based on the Yr1995 experiment described above with the following modifications: 1) Yr1995-w0 is an experiment with vertical velocity set to zero, 2) Yr1995-k0 is an experiment with vertical diffusivity set to zero, and 3) Yr1995-ice0 is an experiment with no sea-ice cover (i.e., purely open-water conditions).

Figure 10b shows $mCDR_{eff}$ for the Yr1995 experiment at the end of simulation, plotted against the central latitude of each deployment location, along with profiles of timemean vertical velocity and vertical diffusivity. Figure 10c shows profiles of normalized Alk perturbation (i.e., $\Delta \widehat{Alk}$ normalized by the maximum value of all experiments) at the end of simulation to show the vertical extent of the OAE perturbation.

We find that $mCDR_{eff}$ is strongly dependent on deployment location (Fig. 10b), with the largest values found near the equator, at subpolar latitudes in the southern hemisphere (between approximately 60–50°S), and at mid-latitudes in the northern hemisphere (between approximately 40–50°N). The lowest values (less than 0.5) are generally found in subtropical regions and near the poles. High $mCDR_{eff}$ values generally coincide with ⁸¹⁹ upwelling regions (Fig. 10b), where Alk perturbations remain near the surface (Fig. 10c). ⁸²⁰ Low $mCDR_{eff}$ values are associated with downwelling regions for which the Alk pertur-⁸²¹ bations are either transported to depth or spread over a substantial vertical extent (Fig. 10b-⁸²² c).

Figure 11 shows $mCDR_{eff}$ for the three deployment seasons (Figure 11a) and three 823 sensitivity experiments (Figure 11b). For reference, Figure 11c shows $mCDR_{pot}$ and sea-824 ice cover. All quantities are plotted as a function of deployment latitude. We find that 825 $mCDR_{eff}$ has a strong dependence on deployment season in the mid-latitudes and sub-826 tropics. Summer months are generally associated with higher efficiency compared to win-827 ter, which is consistent with the pulse experiments for NAS and ACC (see Section 3.3). 828 The $mCDR_{eff}$ is up to 0.3 higher in summer compared to winter, which is also consis-829 tent with the seasonality of $mCDR_{eff}$ for the NAS pulse experiments (Sec. 3.3.2). 830

We also find that sea-ice cover strongly suppresses $mCDR_{eff}$. The experiments shown in Figure 11b demonstrate that for polar OAE deployments in the southern hemisphere, which are under the influence of seasonal sea ice, the sea-ice cover prevents CO_2 uptake and therefore these regions are associated with low values of $mCDR_{eff}$. Removing seaice cover in rapid-mCDR (Figure 11b, orange line) increases $mCDR_{eff}$ to values close to one south of roughly 50°S. Therefore, our simulations suggest that mCDR efforts will be much less efficient in this and other sea-ice-covered regions.

From the two dominant ocean circulation processes, vertical velocity and diffusivity, we find that vertical velocity dominates low-efficiency regions. That is, the vertical diffusivity is of secondary importance. There is only a small increase of $mCDR_{eff}$ with respect to the Yr1995 experiment if the vertical diffusivity is set to zero (Figure 11b, purple line). However, if the vertical velocity is set to zero $mCDR_{eff}$ becomes close to one for most of the deployment sites (Figure 11b, green line), except for sea-ice-covered regions in the southern hemisphere.



Figure 10. (a) Location of rapid-mCDR deployments across the Pacific Ocean; (b) $mCDR_{eff}$ at the end of 2017 for Yr1995 experiment (solid black line), profile of average vertical velocity (colored contours), and vertical diffusivity (gray contour lines with units of 10^{-2} m² s⁻¹); (c) $mCDR_{eff}$ at the end of 2017 for Yr1995 experiment (solid black line) and Alk perturbation normalized by the maximum value of all experiments ($\Delta \widehat{Alk}$; colored contours).



Figure 11. Pacific Ocean vertical sections of $mCDR_{eff}$ at the end of 2017 for (a) 3 different pulse deployment seasons (Jul1995, Jan1995, and Yr1995). (b) Experiments with vertical velocity and diffusivity set to zero (Yr1995-w0 and Yr1995-k0, respectively) and simulation without sea-ice forcing (Yr1995-ice0). (c) Average $mCDR_{pot}$ and variability over the deployment site (solid black lines and gray shading, respectively); these are computed from daily-mean values and time-mean sea-ice cover. All values are taken from and shown at the central latitude of the deployment location.

⁸⁴⁵ 5 Summary and Discussion

ECCO-Darwin is an open-source, data-constrained ocean model designed to inte-846 grate physical and biogeochemical processes in a dynamically-consistent framework. Its 847 use of adjoint-based data assimilation for physical processes enables the model to fit global-848 ocean observations without relying on non-physical nudging or incremental adjustments 849 (Forget, Fukumori, et al., 2015; Carroll et al., 2020). This approach preserves the inter-850 nal consistency of ocean physics and biogeochemistry, allowing for fully-closed budgets 851 of conserved properties, which is an essential capability for mechanistic studies and at-852 tribution of carbon fluxes in mCDR research. Furthermore, ECCO-Darwin's ability to 853 constrain both circulation and biogeochemistry with observations enhances confidence 854 in its simulation of ocean dynamics and carbon cycling, making it especially well suited 855 for evaluating the efficacy and impacts of mCDR strategies. 856

In this work, we designed a series of virtual ECCO-Darwin OAE deployments to 857 investigate variability of mCDR efficiency (i.e. the normalized net CO₂ uptake) across 858 archetypal ocean circulation regimes. For two representative regions (i.e. in the North 859 Atlantic subpolar gyre and over the Antarctic Circumpolar Current; NAS and ACC) we 860 compare mCDR efficiency with similar experiments from a different model described by 861 Zhou et al. (2025) (Supporting Material, Figure S9). In both regions, ECCO-Darwin sim-862 ulates higher mCDR efficiencies, with the largest difference observed in the NAS. This 863 may reflect ECCO-Darwin's data-constrained treatment of vertical mixing, mixed layer 864 depth (MLD), and the air-sea disequilibrium (pCO_2^{aq}) , which are critical to OAE out-865 comes. Further inter-model comparisons are needed to better understand the processes 866 driving mCDR efficiency and to identify sources of uncertainty across modeling frame-867 works. 868

While our results offer valuable insight into the variability of mCDR efficiency across 869 major open-ocean circulation regimes, several key limitations remain, alongside oppor-870 tunities for targeted improvements. To more accurately represent specific OAE deploy-871 ments, future work should incorporate critical biogeochemical interactions between OAE 872 materials and seawater, including mineral dissolution and precipitation processes (e.g., 873 Fennel et al., 2023). Simulating mineral-based deployments and tracking their dissolu-874 tion products (e.g., Si and Fe) is also important due to potential ecological impacts (Bach 875 et al., 2019). In polar regions, more realistic representations of air-sea CO₂ exchange—particularly 876

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through sea-ice cracks and leads—could improve flux estimates (Loose & Schlosser, 2011;
Søren et al., 2011). Our current experiments are limited to open-ocean conditions and
do not account for coastal environments. Accurately capturing nearshore OAE deployments will likely require high-resolution regional models or unstructured grid approaches
capable of resolving coastal, estuarine, and near-source dynamics (Ward et al., 2020).

We use our ECCO-Darwin results to motivate and develop a user-friendly 1D model, 882 rapid-mCDR, for rapid quantification of net CO₂ uptake and mCDR efficiency. Users 883 can simulate virtual OAE deployments in various ocean conditions without the need for 884 supercomputing resources — which is a key advantage compared to more complex ECCO-885 Darwin simulations. Combining the 1D model approach with already-published output 886 from a numerical ocean biogeochemistry model, such as ECCO-Darwin (see the Open 887 Research Section), permits characterization of mCDR efficiency for any OAE deployment. 888 Although rapid-mCDR is a simplified model, it reproduces ECCO-Darwin mCDR ex-889 periments relatively well, with the exception of the deployment location in the Tropi-890 cal Pacific equatorial upwelling (EU). At the two deployment sites (NAS and ACC), the 891 discrepancies between ECCO-Darwin and rapid-mCDR are smaller than those between 892 ECCO-Darwin and Zhou et al. (2025). The rapid-mCDR model is complementary to the 893 impulse response function approach of Zhou et al. (2025); Yankovsky et al. (2024), as 894 it can provide more insight into the process drivers and can be better tailored to spe-895 cific OAE deployment strategies. 896

Future rapid-mCDR enhancements will focus on improving the representation of 897 horizontal transport, especially in tropical regions, through either Eulerian or Lagrangian 898 approaches (Lange & van Sebille, 2017; Delandmeter & van Sebille, 2019), as our results 899 indicate that the horizontal transport significantly modulates mCDR efficiency for these 900 regions, which can be seen from the difference between the results of the two versions, 901 rapid-mCDR(DeployAve) and rapid-mCDR(TransAve) for the EU deployment. Further-902 more, we are developing a module for mCDR uncertainty quantification using Monte-903 Carlo approaches. We envision that rapid-mCDR will be a valuable tool for rapid early-904 stage evaluation of potential OAE deployments, as well as for projecting OAE efficiency 905 under future climate scenarios. 906

Open Research Section 907

- ECCO-Darwin model output is available at the ECCO Data Portal: http://data.nas 908 .nasa.gov/ecco/ 909
- Model code and platform-independent instructions for running ECCO-Darwin and rapid-910
- mCDR simulations are available at: https://doi.org/10.5281/zenodo.10562714 911

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Supporting Information for "Regional Efficiency of Marine Carbon Removal via Alkalinity Enhancement: Insights from ECCO-Darwin and a 1D Model"

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Text S1. Validation of Baseline ECCO-Darwin Simulation.

Fig. S1 compares key time-mean surface-ocean fields that impact mCDR potential from the baseline ECCO-Darwin simulation against reference datasets. This comparison highlights the essential ocean conditions characterized by both chemical and physical/dynamical processes and provides the evidence that ECCO-Darwin credibly represents the processes crucial for simulating OAE. Reference sea-surface temperature (SST) is derived from optimally-interpolated satellite and in-situ observations using the methodology of Reynolds, Rayner, Smith, Stokes, and Wang (2002). Sea-surface salinity (SSS), dissolved inorganic carbon (DIC), and Alk are from the OceanSODA-ETHZ dataset (Gregor & Gruber, 2021), which leverages a suite of observations and a two-step approach (cluster-regression) to construct gridded monthly-mean fields that represent the global-ocean carbonate system.

The key aspects of ECCO-Darwin shown on Figure S1 are as follows:

• Polarward decrease of SST as well as the zonal gradient observed across ocean basins (Figure S1a). The latter feature is attributed to meridional transport by large-scale ocean gyres.

• Polarward decrease of SSS and *Alk* and maximum values located in subtropical regions associated with high rates of evaporation (Figure S1b,d). The lowest values are located in regions that exhibit significant sea-ice melt and/or intense precipitation.

• Poleward increase of *DIC* with significant hemispheric asymmetry. The lowest *DIC* values are generally found in the tropics, which are associated with increased biological productivity resulting from by upwelling-driven nutrient supply (Figure S1c).

Figure S2 compares key surface-ocean variables from the previously-published ECCO-Darwin LLC 270 solution (Carroll et al., 2020) against the LLC90 ECCO-Darwin version used in this work. The agreement between the two solutions shows that there is no need for further parameter tuning in the LLC90 set-up.

Figure S3 shows the OAE deployment location and time-mean values of surface magnitude of horizontal velocity, vertical velocity and vertical diffusivity. These fields provide the background ocean state onto which OAE is applied.

Figure S4 shows additional validation for the 5 OAE locations: a scatter-plots of DICand Alk profile from baseline ECCO-Darwin simulations against in-situ GLODAPv2.2022 observations (Olsen et al., 2020) at the 5 deployment sites studied in this work. For all five locations, both DIC and Alk from ECCO-Darwin generally reproduce observations, which demonstrates that ECCO-Darwin captures the key biogeochemical variables relevant for OAE studies in these regions.

Text S2. Estimation of mCDR potential.

We estimate $mCDR_{pot}$ following its definition and considering the full carbon chemistry, as:

$$mCDR_{pot} = \frac{\partial DIC}{\partial Alk} \approx \frac{DIC(pCO_2^{aq}, Alk + \delta Alk, SST, SSS) - DIC(pCO_2^{aq}, Alk, SST, SSS)}{\delta Alk}$$
(1)

where DIC is taken as a function of pCO_2^{aq} , Alk, sea surface temperature (SST), and sea surface salinity (SSS), and is estimated using the PyCO2SYS (Humphreys et al., 2022) carbonate system. In this computation, the concentration of borate and minor ions are taken to be a function of salt concentration, as it is usually done. We take

 $\delta Alk = 100 \ \mu \text{mol kg}^{-1}$. The results are not sensitive to the exact value of δAlk and we use the monthly-mean values of the surface- ocean state.

In this approach, $mCDR_{pot}$ can thus be estimated from the baseline state of the ocean (without considering the specific OAE approach) from ECCO-Darwin or any other dataset that include required inputs for Equation 1.

In this work, we estimate $mCDR_{pot}$ from both the baseline ECCO-Darwin and OceanSODA-ETHZ (Gregor & Gruber, 2021) datasets.

Text S3. Budgets of DIC and Alk perturbations due to OAE

To quantify vertical mixing and dynamics of Alk and DIC perturbations and their interaction with OAE-attributed net CO_2 uptake, we derive horizontally averaged equations for Alk and DIC perturbations, as described below. We begin with the budget equations for these two quantities as represented in ECCO-Darwin (Carroll et al., 2022):

$$\frac{\partial DIC}{\partial t} = -\nabla(\vec{u} \cdot DIC) + \nabla K(\nabla DIC) + \frac{\partial DIC}{\partial t}\Big|_{bio} + \frac{\partial DIC}{\partial t}\Big|_{dillution} + \frac{\partial f_C}{\partial z} , \quad (2)$$

$$\frac{\partial Alk}{\partial t} = -\nabla(\vec{u} \cdot Alk) + \nabla K(\nabla Alk) + \frac{\partial Alk}{\partial t}\Big|_{bio} + \frac{\partial Alk}{\partial t}\Big|_{dillution} + \frac{\partial f_A}{\partial z},\tag{3}$$

where symbols \vec{u} and K are the 3-D velocity and diffusivity fields.

The terms on the left-hand-side of Equations 2 and 3 represent tendency terms. The first two terms on the right-hand-side of the two equations are resolved advection and parameterized turbulent and molecular diffusion, the third term (with the subscript *bio*) represents biological impacts, and the fourth term (with the subscript *dillution*) represents dilution due to freshwater flux through precipitation and river runoff, and the last terms represent the air-sea CO_2 exchange and *Alk* flux for *DIC* and *Alk* , respectively.

Next, we horizontally integrate Equations 2 and 3 over the global ocean and compute the difference of the budget terms for the OAE-perturbed and baseline simulation to obtain the following two equations for DIC and Alk perturbations:

$$\frac{\partial}{\partial t} \Delta \widehat{DIC} = \underbrace{-\frac{\partial}{\partial z} \widehat{w \Delta DIC}}_{\text{advection}} + \underbrace{\frac{\partial}{\partial z} \widehat{K \frac{\partial}{\partial z} \Delta DIC}}_{\text{diffusion}} + \underbrace{\frac{\partial}{\partial t} \widehat{\Delta DIC}|_{bio}}_{\text{biology}} + \underbrace{\frac{\partial}{\partial z} \widehat{\Delta f_C}}_{CO_2 \text{ flux}} \text{ and } (4)$$

$$\underbrace{\frac{\partial}{\partial t}\Delta\widehat{Alk}}_{\text{tendency}} = \underbrace{-\frac{\partial}{\partial z}\widehat{w\Delta Alk}}_{\text{advection}} + \underbrace{\frac{\partial}{\partial z}\widehat{K\frac{\partial}{\partial z}\Delta Alk}}_{\text{diffusion}} + \underbrace{\frac{\partial}{\partial t}\widehat{\Delta Alk}}_{\text{biology}} + \underbrace{\frac{\partial}{\partial z}\widehat{\Delta f_A}}_{\text{OAE }\Delta Alk},$$
(5)

where Alk and DIC perturbations between OAE and baseline simulations are represented by ΔAlk and ΔDIC , respectively and the $\hat{\varphi}$ represents the horiontal integral of variable φ over the global ocean. To derive Equations 4 and 5, we assume that ocean circulation and Alk/DIC dilution are not impacted by the OAE deployment, and that for advective and diffusive terms the horizontal components become zero.

For the 5 continuous Alk experiments, Figs. S5 and S6 show the profiles of budget terms for $\Delta \widehat{DIC}$ and $\Delta \widehat{Alk}$. For all of the OAE deployments the response of biological processes was insignificant — the biological source terms were at least 3 orders of magnitude lower compared to the tendency terms for both $\Delta \widehat{DIC}$ and $\Delta \widehat{Alk}$ and are therefore not shown. For clarity, the budget terms are shown only for the last 5 years of simulation; however, they are representative of the entire simulation period.

In addition, Figs S5 and S6 show the mixed layer depth (MLD) as indicative of the interface that separates highly turbulent and relatively well-mixed near-surface layer from the stably-stratified ocean below. The MLD is diagnosed from daily averaged values of thermodynamic fields, and since there is considerable uncertainty in characterization of

MLD we plot its values from *Boyer* (de Boyer Montégut et al., 2004), *Suga* (Suga & Hanawa, 1990), and *Kara* (Kara et al., 2003) methods.

For the NAS deployment, MLD varies most strongly and is between 400–900-m deep during winter and early spring and shoals to about 50-m during summer. The three MLD depth computations differ, especially during winter and early spring when the MLD is deepest. Boyer and Suga MLD differ the most, with Boyer being consistently shallower, while Kara MLD lies between these two extremes. For NAS, vertical diffusion transports $\Delta \widehat{DIC}$ and $\Delta \widehat{Alk}$ from the surface via a deepening of the MLD, which indicates presence of strong vertical mixing. This transport is strongest when the MLD deepens substantially during winter. Vertical advection transports near-surface $\Delta \widehat{DIC}$ and $\Delta \widehat{Alk}$ into upperocean layers (roughly 100-m deep), while it is also responsible for a sink of ΔDIC and ΔAlk throughout much of the deeper layer between 200–800 m. This advective transport appears to be fairly independent of MLD dynamics. The tendency of near-surface ΔAlk exhibits a strong seasonal cycle: $\Delta \widehat{Alk}$ generally increases when the MLD shoals (due to OAEAlk addition). However, when the MLD deepens, even though the Alk is added in the near surface layer, the $\Delta \widehat{Alk}$ decreases at the expense of vertical mixing associated with a deepening of the MLD. Similar dynamics occur for ΔDIC , except that the ΔDIC budget is impacted by atmospheric CO_2 which also has a strong seasonal cycle peaking in late fall and early winter — just before the MLD begins to deepen.

WBC, ACC, and STG sites share many similar characteristics, except that for ACC the MLD is out of phase because the deployment is located in the southern hemisphere. MLD dynamics are dominated by strong seasonality and deepen to roughly 200 m during spring and are shallowest during late summer for the respective hemispheres. For EU, the

MLD has weaker seasonality. The three MLD criteria agree well in terms of MLD depth and seasonal variability. As for NAS, the deepening of the MLD is associated with strong vertical diffusion of ΔDIC and ΔAlk from the surface within the MLD. Here vertical diffusion tend to overshoot the MLD and indicates either underestimation of MLD by all three MLD criterion or strong vertical mixing that extends beyond the MLD. For both of these locations, advection transports both ΔAlk and ΔDIC from near-surface waters to depth. While ACC has weak seasonality in advective transport, it is substantial for WBC. As for NAS, surface-ocean fCO_2 has strong seasonality, which is presumably related to the seasonality of MLD and advective term. This seasonality is less apparent for ACC and STG. We note that the seasonality of fCO_2 can also be impacted by CO_2 piston velocity.

For EU, due to its location in the tropics, has no discernible seasonal cycle of MLD. Here diffusion generally mixes $\Delta \widehat{Alk}$ and $\Delta \widehat{DIC}$ from the surface downwards and advection, while it exhibit significant temporal variations, generally transports $\Delta \widehat{Alk}$ and $\Delta \widehat{DIC}$ towards the surface. This site also has seasonal transport of $\Delta \widehat{Alk}$ and $\Delta \widehat{DIC}$ below 150-m depth. EU is associated with strong multi-annual variability in pCO_2^{aq} . For the 5-year shown in Figure S5, the pCO_2^{aq} is significantly increased around the start of year 2016.

Text S4. Additional comparison of ECCO-Darwin and rapid-mCDR

While the main comparison of ECCO-Darwin against rapid-mCDR is shown in the main text, Figure S7 shows additional comparison of vertically-resolved $mCDR_{equil}$ between ECCO-Darwin and rapid-mCDR, along with its time evolution for all five continuous experiments and for both both versions of horizontal averaging (rapid-mCDR(DeployAve) and rapid-mCDR(TransAve) see main text for details). For all five experiments, rapid-mCDR generally captures the ECCO-Darwin profiles of $mCDR_{equil}$. In general, we find that the values with rapid-mCDR(TransAve) are closer to ECCO-Darwin compared to values from rapid-mCDR(DeployAve) which is expected as the former ones accounts for the horizontal advection of OAE perturbation.

Text S5. Additional figures

For the five continuous OAE experiments, Figure S8a shows the maximum pH modification due to OAE for all five continuous experiments and the time series of the depth that separates OAE-impacted waters from unmodified waters, and Figure S8b shows the time series of the depth that separated OAE-impacted waters from unmodified waters (see main text for definition and details).

Figure S9 compares the net CO₂ uptake efficiency, η , from monthly and yearly NAS and ACC deployments in ECCO-Darwin to the range of efficiencies derived from the four closest polygons in Zhou et al. (2025), obtained from the CarbonPlan website¹. The specific polygons used for this comparison are listed in Table S1. For this comparison, we assume that the deployments in Zhou et al. (2025) were conducted in the year 1995. To estimate the yearly deployment efficiency, we averaged efficiency values from four representative months: January, April, July, and October.

As shown in Figure S9, the overall efficiency η is higher in ECCO-Darwin. However, the seasonal variation in efficiency is comparable between the two simulations. Further investigation is needed to attribute these differences to the underlying processes.

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Notes

1. https://carbonplan.org/research/oae-efficiency

(a) SST

(b) **SSS**



(d) Alk ¹⁸⁰⁰ ¹⁸⁵⁰ 2050 2100 2150 1900 1950 2000 2400 [μmol/kg] 2100 2350 2150 2250 2200 2300

Comparison of time-mean (from January 1995 to December 2017) surface-Figure S1. ocean fields from the baseline ECCO-Darwin simulation against reference (a) sea-surface temperature (SST), (b) sea-surface salinity (SSS), (c) DIC, and (d) Alk. Reference SST is from Reynolds et al. (2002); all other reference fields are from OceanSODA-ETHZ (Gregor & Gruber, 2021).

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Figure S2. Comparison of time-mean (1995–2017) surface-ocean fields from ECCO-Darwin LLC 270 (Carroll et al., 2020) and the baseline ECCO-Darwin (LLC90 solution) used in this paper.



Figure S3. (a) OAE deployment sites and time-mean values (from January 1995 to December 2017) of (b) magnitude of surface-ocean horizontal velocity, (c) average vertical velocity in the upper 100 m, and (d) average vertical diffusivity in the upper 100 m.



Figure S4. Comparison of the baseline ECCO-Darwin *DIC* and *Alk* against all GLODAPv2.2022 observations (Lauvset et al., 2021) at the 5 deployment sites. The x-axis shows observations and y-axis shows the corresponding monthly averaged model value taken at the closest space-time location.



Figure S5. Horizontally-integrated budget terms from ΔDIC (Equation 4) for the 5 continuous OAE experiments over the last 5 years of simulation. Budget terms include: tendency, diffusion, advection, and air-sea CO₂ flux. Biological source terms are negligible and not shown. Three different mixed layer depth (black lines) are computed using Boyer, Suga, and Kara diagnostics and we plot the spatially averaged values over the OAE deployment sites.

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Figure S6. Horizontally-integrated budget terms for $\Delta \widehat{Alk}$ (Equation 5) for the 5 continuous OAE experiments over the last 5 years of simulation. Budget terms include: tendency, diffusion, and advection. Biological source terms are not shown because they are negligible; prescribed surface-ocean Alk flux is constant and is also not shown. Three different mixed layer depth (black lines) are computed using Boyer, Suga, and Kara diagnostics and we plot the spatially averaged values over the OAE deployment sites.



 $mCDR_{equil}$ from ECCO-Darwin (left panel) and both versions of rapid-mCDR (middle and right panels).

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Figure S8. Continious OAE experiments: (a) Maximum pH perturbation across time and depth (maximum Δ pH) due to OAE for the 5 continuous experiments. Only values above 0.0025 are shown. Isolines represent maximum ΔpH values of 0.01, 0.02, 0.03, and 0.04. (b) Time series of the depth that separates OAE-impacted waters from unmodified waters. This depth is such that 95% of ejected alkalinity stays above it.

ED deployments	Polygons from Zhou et al. (2025)
NAS	32, 52, 128, 138
ACC	509,530,629,635

Table S1.Polygon indices from Zhou et al. (2025) on CarbonPlan website used forcomparison with ECCO-Darwin deployments.



Figure S9. Net CO₂ Uptake Efficiency (η) from ECCO-Darwin: monthly pulse Deployments (July 1995 – Blue; January 1995 – Red), Yearly 1995 Deployment (Black), and Zhou et al. (2025) Ranges (Shaded Areas). The Zhou et al. (2025) ranges are derived from the spread of simulations from the four nearest polygons to our deployment sites (polygon indices are shown in Table S1). The yearly ECCO-Darwin deployment is compared to the mean efficiency of four monthly deployments from Zhou et al. (2025). Note that the experiments of Zhou et al. (2025) were initialized in the year 1999, but the initial year is shifted to 1995 on the plot for comparison. Panel (a) for NAS and (b) for ACC deployment locations.